The "birth hump": A shape decomposition of perinatal excess mortality

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Abstract

We characterise the mortality pattern over gestational age for a cohort of fetuses as they pass the transition of birth. This transition leaves a mark on the mortality trajectory visible as a "birth-hump" — a temporary increase in the risk of either fetal or perinatal death centered around an age of 38 weeks of gestation. Using competing risks survival analysis, we exploit this pattern to quantify the risk of death contributed by the birth transition itself.

1. Introduction

In this paper, descriptive findings on the feto-infant mortality trajectory and the associated phenomenon of a "birth hump" are presented.

The different segments of a birth cohort's mortality trajectory have been thoroughly mapped starting with the sudden decline in the risk of death after a peak at birth (e.g., Bourgeois-Pichat 1951; Galley and Woods 1999; Berrut et al. 2016), the arrival at minimum risk in late childhood (Ebeling 2018), the "hump-shaped" excess mortality in adolescence (e.g., Thiele 1871; Goldstein 2011; Remund et al. 2018) and the exponential increase in the mortality hazard over much of the adult life (e.g., Gompertz 1825) which eventually flattens (e.g., Perks 1932; Vaupel 1997; Horiuchi and Wilmoth 1998) and then plateaus among the oldest-old (e.g., Gampe 2010; Barbi et al. 2018). Similar investigations have been made concerning the changing mortality risk of the unborn child over the age of a pregnancy (e.g., Shapiro et al. 1962; Bakketeig et al. 1978; Goldhaber and Fireman 1991; Carlson et al. 1999; Woods 2009).

Both survival scenarios, fetal and infant, meet at the point of birth but are nonetheless fundamentally separated by the use of different timescales. While prenatal mortality is indexed by gestational age, commonly measured as the weeks since the last menstrual period of the pregnant woman, the survival of those born alive is followed over chronological age, i.e., time since birth. Such a strict separation of populations along the dividing line of birth makes this critical transition invisible in the study of mortality, delegating to it either the role of a right censoring or a point of entry into the risk set. An alternative perspective allows bridging the feto-infant gap by situating birth within the lifecycle of a cohort of unborn children whose survival is tracked over the age of gestation into infancy.

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By marking the vital events of fetal death, birth and infant death on a common age scale the risky transition of birth becomes an event *within* the temporal observation horizon and its effect on the survival of a cohort on the onset of life can be studied by defining a feto-infant mortality trajectory: the combined risk of fetal or infant death among all members of a conception cohort still alive at a given week of gestation.

Figure 1: The feto-infant mortality trajectory over gestational age for a U.S. cohort of fetuses conceived in 2009, surviving until fetal viability and followed over the next 52 weeks. The risk of feto-infant death among the survivors of the cohort declines exponentially over age interrupted only by a "birth hump."



Figure 1 shows gestation specific mortality rates for a cohort of children conceived in 2009 and either born or registered as an infant or fetal death in the U.S. The denominator of the rate is based upon all members of the conception cohort alive (either as fetus or infant) during a given week of gestation whereas the numerator includes all fetal- and infant deaths within the same week. The feto-infant mortality trajectory constructed from these rates thus measures the changing risk of *any* adverse pregnancy outcome for the 52 weeks following gestational age 24, commonly defined as the "limit of viability" (Seri and Evans 2008). The trajectory may be interpreted as the changing hazard of death for a cohort as its members pass the tumultuous transition period from fetus to infant. An exponential decline in mortality characterizes this period, interrupted only by hump-shaped excess mortality associated with the age-distribution of deliveries.

Mortality trajectories that stretch across the feto-infant gap have been proposed several times but never entirely realized. In his seminal work on "ontogenescence," – the declining risk of death over age before maturity – Levitis (2011) considers the hazard of death on an age continuum from conception until adolescence with the event of birth acting as a "transitional shock." By using a negative time scale before birth and positive after, Levitis implicitly assumes all births to occur at the same time post-conception – a simplifying assumption which naturally leads to a spurious "birth spike" rather than a "birth hump." Williamson and Woods (2003) and Woods (2009) model the cumulative risk of death of a cohort from conception until the first birthday and use weeks of gestation as time scale throughout the complete follow-up. As Williamson and Wood's model is based on previously published disjoint fetal- and infant life tables, they too assume all births to take place at full-term.

The joint consideration of fetal and infant death is perhaps most prominently expressed in the perinatal mortality rate, commonly defined as the sum of all fetal deaths and infant deaths during the first seven days of life over the number of births within a year (World Health Organization 2006). The necessity for such a measure arose from the uncertainty regarding the classification of a death as stillborn or infant due to both varying legal requirements and the subjective judgment of the pediatrician. Designed as a simple and therefore widely applicable indicator, the perinatal mortality rate does not consider the time dimension of pregnancy, nor does it permit a survival analytic interpretation as the denominator is not the population at risk.

Fetal life tables add both a time dimension and a survival interpretation to the analysis of pregnancy outcomes via the introduction of an "ongoing pregnancies" denominator (e.g., Shapiro et al. 1962; French and Bierman 1962; Bakketeig et al. 1978; Goldhaber and Fireman 1991). These life-tables report the probability of fetal death among the intrauterine survivors to some week of gestation. In an influential article Yudkin et al. (1987) advertise the use of a "fetuses at risk" denominator for the analysis of perinatal mortality by gestational age leading to a range of age-specific mortality indices that include compound fetal- and infant death endpoints (Kristensen and Mac 1992; Smith 2001; Platt et al. 2004; Joseph 2004; Smith 2005; Joseph 2007). Kristensen and Mac (1992) follows a cohort of fetuses from week 31 of gestation into infancy until week 76 and calculates a corresponding survival curve. The ratio of fetal- and neonatal¹ deaths over fetuses at risk by week of gestation is advertised by Joseph (2007) as the proper "causal" framework to the study of perinatal mortality. Making a similar argument Platt et al. (2004) propose a Cox regression model over age of gestation featuring a combined feto-infant death endpoint.

This paper contributes to the aforementioned literature on survival analysis *around* the onset of life by studying the age pattern of mortality in a cohort of fetuses as they transition into infancy. A distinct phenomenon of this perinatal mortality trajectory is the "birth hump." Via simple decomposition analysis, we show how fetal-, neonatal, and postneonatal mortality and the probability of live birth all act together to form the "hump." In a second step, we quantify the magnitude of the "hump" by proposing that the distinctive shape of feto-infant mortality on a cohort level is the result of two competing hazards:

¹ In this paper we use the term "neonatal" as referring to the first week of life.

An "ontogenescent" hazard, due to causes with a declining incidence, and a "transitional" component, due to birth-related causes. We propose the probability of a fetus at 24 weeks of age to survive the following 12 months as a summary of the feto-infant mortality trajectory and ask how differences in this indicator across cohorts and between population strata are driven by changes in the shape of the gestational age pattern of feto-infant mortality.

2. Data and Methods

In this paper, we analyze U.S. fetal deaths, births, and infant deaths over the age of gestation. The data basis for this analysis consists of the birth certificates for the U.S. birth cohorts 1989/1990, 1999/2000, 2009/2010, 2014/2015, the linked infant death certificates where applicable, and the fetal death certificates for the years 1989/1990, 1999/2000, 2009/2010 and 2014/2015. Digitized versions of the certificates are provided by the National Center for Health Statistics in the form of the "Birth Cohort Linked Birth – Infant Death Data Files" (National Center for Health Statistics 2016a) and the "Fetal Death Data Files" (National Center for Health Statistics 2016b, see also Martin and Hoyert (2002) for an introduction).

To analyze the gestational age mortality trajectory of a cohort of fetuses as they transition into life, we construct three conception cohorts of all fetuses conceived during the years 1989, 1999, and 2009 respectively. The 2009 cohort is further stratified by sex and maternal origin, two characteristics which are available on most birth-, fetal- and infant death certificates and serve to show how the phenomenon of the birth hump and the ontogenescent feto-infant mortality decline compares across key demographics.

Causes of death for the 2014 cohort are categorised into 10 main groups: Infections & parasites, maternal complications, placenta/cord/membrane/labour complications, prematurity, nonspecific stillbirths, sudden infant death, accidents and violence, severe and less severe congenital anomalies & neoplasms, and other. Congenital anomalies are classified as severe if there is little or no treatment and the chance of survival is very low. Detailed information on the coding of causes of death can be found in Table 10.

Only fetuses who survived until week 24 of gestation, commonly defined as the "age of viability," are considered in this study. Reporting guidelines and practice for fetal death vary across states. A left-truncation age of 24 serves to rectify these differences. It is chosen because based on evidence that under-reporting drastically increases already at week 23 (Greb et al. 1987)². Furthermore, a relatively late left-truncation age serves to minimize the bias due to the unknown numbers of induced abortions.

The initial size of the fetal-cohort at the beginning of week 24 is calculated via the "extinct cohort" method (Bakketeig et al. 1978; Feldman 1992) by adding all life-births within a conception cohort to all fetal deaths at weeks 24+. This is due to the simple observation that a life-birth at week of gestation t was a fetus prior to t.

² While their study dates back to 1987 we found evidence for the continued under-registration of fetal deaths in the U.S. prior to week 24 in the form of declining fetal death rates going from week 23 to 20 which lacks a biological explanation.

Using a multi-state life table, we follow the initial fetal population at week 24 for 52 weeks counting for each week *t* fetal deaths, neonatal deaths, post-neonatal deaths, and the corresponding population of survivors and their distribution across these three states. Distinguishing fetuses, newborns and infants who survived the first week of life then allows to decompose week-to-week changes in the combined feto-infant mortality rates $m_t = \frac{\# \text{ fetal or infant deaths at week } t}{\text{Total feto-infant time at risk during week } t}$ into changes due to a shifting distribution of fetuses, vs. neonates vs. post-neonates, and changes due to declining or increasing mortality rates within each state. Such a decomposition explains the "birth hump" in terms of the perinatal population dynamics. The Kitagawa method (Kitagawa 1955) is used to perform the decomposition.

Assuming a competing risks model (Table 1) where death is either the result from causes which exhibit gradually declining incidence over gestation (e.g., extreme prematurity, in-utero fatalities due to congenital anomalies) or from causes increasing in incidence as full-term approaches (e.g., obstetric causes), we quantify the share of fetal- or infant deaths over the one-year follow-up from fetal viability which can be attributed to the "birth-hump."

We define F(52), the probability for a fetus alive at the 24th week of pregnancy to die in the following year, as a summary indicator of adverse pregnancy outcomes. In order to elucidate how the "shape" of the feto-infant hazard trajectory determines population differences in overall feto-infant death counts, we decompose differences in F(52) between two populations into differences due to the initial magnitude of mortality at the age of fetal viability, differences due to the rate of mortality decline over gestational age, and differences due to the location, shape, and magnitude of the "birth hump" component. This decomposition is performed via the Horiuchi decomposition (Horiuchi et al. 2008) of the differences in F(52) as predicted by the model outlined in Table 1.

Table 1: Parametric specification of the feto-infant mortality trajectory over age of gestation and derived quantities.

Ontogenescent hazard The instantaneous risk of fetal or infant death at gestational age t = x + 24 due to causes with a continuously declining incidence.

$$h^{O}(x) = a_1 \exp(-bx)$$

Cumulative ontogenescent hazard

feto-infant death at age of fetal viability.

hump.

$$H^{O}(x) = \int_{0}^{x} h^{O}(s) \, ds = \frac{a_{1} - a_{1} \exp(-bx)}{b}$$

a1 Level of feto-infant mortality The approximate hazard of

b Rate of ontogenescence The relative rate of feto-infant

mortality decline over gestational age in absence of birth

Transitional hazard The instantaneous risk of fetal or infant death at gestational age x due to causes associated with the timing of onset of labor.

$$h^{\mathrm{T}}(x) = a_2 \exp\left(-\frac{(x-c)^2}{2\sigma^2}\right)$$

Cumulative transitional hazard

$$H^{\mathrm{T}}(x) = \int_0^x h^{\mathrm{T}}(x) \,\mathrm{d}s = a_2 \sigma \sqrt{\pi/2} \left[\mathrm{erf}(A) + \mathrm{erf}(B) \right],$$

where $A = \frac{c}{\sqrt{2}\sigma}$, $B = \frac{x-c}{\sqrt{2}\sigma}$, and $erf(\cdot)$ is the Gaussian error function.

a2 Magnitude of birth hump The instantaneous risk of fetal or infant death contributed by the birth-hump component at its peak.

c Location of birth hump

The gestational age t = c + 24 coinciding with the peak of the risk of fetal or infant death contributed by the birth-hump component.

 σ Spread of transitional shock The curvature of the risk of feto-infant death around its peak. Higher values flatten the birth hump.

 $\pi_k^{\rm T}(x) = \frac{F_k^{\rm T}(x)}{F^{\rm T}(x)}$

Combined haza	rd
Hazard of feto-infant death The instantaneous risk of fetal or infant death x weeks past fetal viability.	$h(x) = h^{O}(x) + h^{T}(x)$
<i>Feto-infant survival curve</i> The probability of surviving <i>x</i> weeks past fetal-viability.	$S(x) = \exp\left(-H^{O}(x) - H^{T}(x)\right)$
Cumulative incidence of feto-infant death Probability of fetal or infant death x weeks past fetal-viability. $F(x) = 1 - S(x)$	
Competing risks inf	erence
Cumulative incidence of feto-infant death due to causes as- sociated with the timing of onset of labor.	$F^{\mathrm{T}}(x) = \int_0^x S(s) h^{\mathrm{T}}(s) \mathrm{d}s$
Share of feto-infant deaths over <i>x</i> weeks following fetal viability contributed by the "birth hump".	$\rho(x) = \frac{F^{\mathrm{T}}(x)}{F(x)}$

Share of feto-infant deaths over x weeks following fetal viability due to specific cause k on all deaths contributed by "birth hump" (cause-of-death decomposition).

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3. Results

3.1 Feto-infant population dynamics over gestational age

The gestational age trajectory of feto-infant mortality as shown in Figure 2A may be segmented into a decline from week 24 to 33, a steep increase from week 33 to 39, a steep decrease from week 39 to 45, and a more gradual decrease over weeks 45 to 72. Throughout these four segments, the population composition shifts from a cohort of fetuses to a cohort with a substantial share of neonates to a cohort entirely composed of postneonates. Fetal mortality rates decline until week 32 and start to increase drastically into post-term, neonatal mortality declines until week 40, and then plateaus and postneonatal mortality declines continuously over the entire observation period (Figure 2B). As shown by the Kitagawa decomposition in Table 2, the particular shape of the feto-infant mortality trajectory is the result of both the aforementioned changes in composition and rates.

Table 2: Decomposition of the change in combined feto-infant mortality over gestational age into contributions due to changing risk of death among fetuses, newborns, and post-neonates and the changing structure of the population along these dimensions. Percent relative change is given in parenthesis.

Week	25	\rightarrow	33	\rightarrow	39	\rightarrow	45	\rightarrow	72
Mortality by	stratum in	deaths per 1	00,000 pe	erson-weeks e	xposure				
Fetus	25.6	(-22.4)	19.9	(+144)	48.6	(+128)	111.1		
Neonatal	16,774	(-95.7)	713	(-94.2)	41.2	(+53.5)	63.2		
Postneonatal	6,392	(-97.1)	187	(-87.1)	24.1	(-59.3)	9.8	(-78.8)	2.1
Relative expo	sure by st	ratum							
Fetus	.998	(-2.6)	.973	(-51.7)	.470	(-98.9)	.005	(-100)	0
Neonatal	<.001	(+732)	.008	(+2901)	23.2	(-97.6)	.006	(-100)	0
Postneonatal	<.001	(+5, 130)	.019	(+1443)	.298	(+232)	.989	(+1.1)	1
Combined fet	to-infant n	ortality							
	43.6	(-34.6)	28.5	(+38.9)	39.6	(-73.2)	10.6	(-80.4)	2.1
Absolute cha	nge in feto	-infant mort	ality due	to differences	in				
Composition		+121.2		+96.7		-37.2		-0.39	
Rates		-136.3		-85.6		+8.2		-8.2	
Total Δ		-15.1		+11.1		-28.9		-8.6	

Weeks 25 to 33: pre-term decline. Feto-infant mortality declines by 34.6 percent over the nine weeks following the age of fetal-viability. The overwhelming share of the decline can be attributed to the lessening burden of prematurity reflected in the 95.7% decline of neonatal mortality: Infants born at week 25 have a risk of death elevated by a factor of 654 compared to the fetal population at the same age whereas at week 33 this neonate penalty is reduced to a factor of 35.8. However, the increasing share of neonates from less than a percent to 1.9 percent counterbalances the effect of the reduction in neonatal mortality on the differential in feto-infant mortality.

Weeks 33 to 39: increase towards full-term. Approaching full-term, feto-infant mortality reverses its trend and increases by 38.9 percent. Part of this increase is due to the increase in fetal death rates by more than 144 percent, an effect that is, in turn, mediated by the declining share of the fetal population in the cohort by 51.7 percent. Neonatal mortality

rates continue to be higher compared to fetal mortality prior to week 39 (Figure 2C), and thus the rapidly increasing share of newborns contributes to the increase in combined feto-infant mortality.

Weeks 39 to 45: post-term decline. While mortality increases post-term for both fetuses and neonates, it is the quickly vanishing share of both sub-populations that, along with declining rates of post-neonatal mortality, drives the steep decline in feto-infant mortality following full-term.

Weeks 45 to 72: post-neonatal decline. With no remaining fetuses or neonates in the population, the feto-infant mortality trajectory is completely determined by the declining mortality of the post-neonatal population.

Figure 2: Rates of fetal death, neonatal death, and post-neonatal death over weeks of gestational age as calculated for the cohort of U.S. fetuses conceived in 2009. The shaded background shows the distribution of survivors among the three states.



3.2 Competing risks feto-infant mortality trajectories

Males have a higher probability of death in the 52 weeks following fetal viability (Figure 3A). Out of 100,000 male fetuses of the 2009 U.S. conception cohort surviving until 24 weeks of gestation $851-878^3$ (one out of 114-116) will not survive the following year, compared to 739–763, (one out of 131-135) female deaths over the same period. Thus, the male probability of feto-infant death is 12.6-17.8 percent higher than that of females. Most of this difference in survival is explained by a higher hazard level in males as measured by the a_1 parameter: Ignoring the slightly earlier peak of the birth hump in males, the male hazard of feto-infant death is consistently higher across the 52 weeks of post-viability gestational age. The hazard of feto-infant death declines with a rate of 6.5-6.8 percent per additional week of gestation for males and 7.0-7.3 percent for females. The higher rate of ontogenescence among females substantially contributes to the sex-difference in one-year post-viability survival, while different magnitude and spread of the "birth hump" exhibit only a marginal and non-significant contribution. For additional parameter estimates see Tables 4 and 7.

Feto-infant survival improves considerably in the U.S. from 1989 to 2009. Out of 100,000 fetuses conceived in 1989 and reaching the age of viability 1,196–1,219 (one in 82–84), do not survive the following 52 weeks. This number drops to 969–990 (one in 101–103) deaths for the 1999 cohort and further down to 800–818 (one out of 122–125) deaths for conceptions in 2009. The 17.8–20.1 percent improvement in feto-infant survival between 1989 and 1999 is mainly explained by an increase in the rate of ontogenescence from approximately 6.1–6.2 percent per additional week of gestation to 7.0–7.2 percent and by a drop in the level of feto-infant mortality from 63–65 to 56–58 deaths per 100,000 person-weeks of exposure at fetal-viability. While the location of the peak "birth-hump" shifts into earlier gestation by about a week, neither magnitude nor spread of the hump change substantially between cohorts 1989 and 1999. Hence, the contribution of the transitional component to the overall improvement in one-year post-viability survival is small.

A different picture emerges for the 16.1–18.6 percent improvement in feto-infant survival between conception cohorts 1999 and 2009, which is primarily driven by a decline in the level of feto-infant mortality from 56–58 to 46–48 deaths per 100,000 person-weeks of exposure at fetal-viability. A substantial reduction in the magnitude of the birth hump from a peak value of 32–35 deaths per 100,000 person-weeks of exposure to 23–25 further contributes to the survival improvements while the rate of ontogenescence remains nearly constant.

³ We report the 95 percent prediction interval around the estimates.

Figure 3: Age trajectories of feto-infant survival A) by sex for the U.S. conception cohort 2009, B) by U.S. conception cohort, C) by maternal origin for the U.S. conception cohort 2009. Fitted (lines) versus life table estimates (points).



There are considerable differences in feto-infant survival by ethnicity of the mother with the hazard of feto-infant death for the cohort of non-Hispanic Black origin consistently being greater than the hazards for the cohort of Hispanic or Non-Hispanic White origin (Figure 3C). In the U.S. conception cohort 2009, out of 100,000 fetuses of non-Hispanic Black origin at pregnancy week 24 an estimated 1,332–1,399 (one in 71–75) either die in-utero or as infants in the following year compared to 679–719 (one in 139–147), and 684–705 (one in 142–146) for fetuses of Hispanic and non-Hispanic white origin respectively. Virtually all of the differences in feto-infant survival between the non-Hispanic Black stratum and the White/Hispanic origin strata are due to differences in the hazard level. Notably, the share of deaths attributable to the birth-hump is substantially lower in the non-Hispanic Black stratum (7.5–11.0 percent) compared to the Hispanic (18.7–24.4 percent) and non-Hispanic White (19.1–21.7 percent) strata. For further details see Tables 6 and 9.

3.3 Cause of death decomposition of the "birth hump"

For the cause of death decomposition we analyze all fetuses of the US conception cohort 2014 which survived until a gestational age of 24 (N = 3,999,935). During the 52 week post fetal viability there have been 15,883 fetal and 15,773 infant deaths. Out of those 31,656 feto-infant deaths one out of five deaths is contributed by the "birth-hump" (20.3%).

Figure 4: The hazard of death contributed by the "birth hump" decomposed by cause of death for the U.S. conception cohort 2014.



More than half of the deaths contributed by the "birth hump" are either due to PCML complications (30.6%), i.e. complications in placenta, cord, membrane or labour, or due to congenital malformations and neoplasms (28.5%, Figure 4, Table 3). For a further 15.1% of birth related deaths no specific cause is given. The remainder of birth related deaths distributes across the categories "maternal", "Infections & parasites", and other causes.

The cause-of-death composition of the "birth hump" differs from the overall composition for all feto-infant deaths, with PCML complications and Congenital malformations / Neoplasms being more prominently featured. Conversely, we could not identify a "birth hump" component for deaths due to the Sudden Infant Death Syndrome (SIDS) or accidents and violence. While those two causes jointly contribute 12.9 of all fetal or infant deaths within a year of fetal-viability they overwhelmingly happen after the birth transition has been completed.

Cause-of-death category	Share on "birth hump" deaths (%)	Share on "ontoge- nescent deaths" (%)	Share on all feto- infant deaths (%)
PCML complications	30.6	9.9	16.3
Cong. malformations and neopl. (severe)	22.6	11.9	15.2
Cong. malformations and neopl. (less severe)	5.9	2.5	3.6
Maternal	9.7	6.3	7.3
Infections and parasites	5.8	3.7	4.4
Prematurity	0.8	8.5	6.1
Accidents and violence	0.0	6.8	4.7
SIDS	0.0	11.8	8.2
Unspecific	15.1	17.6	16.8
Other	9.5	21.0	17.4

 Table 3:
 Cause of death contributions to the different components of feto-infant mortality.

Figure 5 shows the hazards by cause of death over gestational age. While the pattern of a monotonic decline in risk disrupted only by a birth hump holds true for PCML complications, congenital malformations and neoplasms as well as unspecific and other causes, there are exceptions to that pattern. The risk of death due to accidents & violence and SIDS increases until after week 40 and then declines without any "hump" feature. This may be related to the fact that both causes of death tend to happen after return home from the birthing clinic.

Figure 5: Age trajectories of feto-infant survival A) by sex for the U.S. conception cohort 2009, B) by U.S. conception cohort, C) by maternal origin for the U.S. conception cohort 2009. Fitted (lines) versus life table estimates (points).



4. Discussion

With the advent of modern obstetric practice, the distinction between fetus and infant stage became malleable and a question of optimal choice: Should we deliver early? Should we perform surgery in-utero? Should we try to prolong the pregnancy? Better and more widely employed prenatal diagnostics made the uterus almost transparent⁴. The feto-infant distinction lost relevance as available knowledge about the degree of maturity, and the presence of congenital disorders informed the future survival prospects of the child, in-utero or not. Isaacson (1996), in a historical study of obstetric texts, identified the "creation of the fetus-infant" – a being separate from the pregnant woman and endowed with a history that begins before birth. The consideration of the feto-infant mortality trajectory over age of gestation naturally arises from the continued blurring of lines that divide the stages of existence. But what does the feto-infant as a concept contribute to the study of mortality? 1. a more realistic quantification of undesired pregnancy outcomes, 2. the phenomenon of a "birth hump," and on a related note, 3. the possibility to model the risk associated with the transition of birth.

Quantifying undesired pregnancy outcomes: A sole focus on rates of infant mortality, fetal mortality or perinatal mortality hides the true incidence of adverse pregnancy outcomes, and the incompatible definition of these measures prohibits to form a simple sum which more truthfully reflects on the loss of life within a pregnancy cohort. By employing the methods of survival analysis, we have calculated that one out of 73 non-Hispanic Black women who conceived in 2009 and continued their pregnancy to the 24th week of gestation are expected to lose their child in the following year. Not only shows this number the continued racial disparity in the prospects of survival at the onset of life when compared to the population average of one in 124; would pregnancy come with the same warnings as prescription drugs, feto-infant death past the age of fetal viability would have to be labeled as a "common" side effect according to the standards put forth in CIOMS Working Groups III and V (1999).

The phenomenon of the "birth hump": Former bio-demographic analyses and descriptions of the age trajectories of combined feto-infant mortality suffered either from a lack of data, the authors being forced to rely instead on rough assumptions and combinations of observations from various populations (Williamson and Woods 2003; Woods 2009; Levitis 2011; Berrut et al. 2016). The detailed micro-data on fetal deaths, births, and infant deaths in the U.S. allowed us to calculate the mortality trajectory of various fetal cohorts as they transition into infancy. Interestingly, the asymmetric sigmoid-shape for the cumulative distribution of feto-infant deaths around term, proposed by Williamson and Woods (2003) on the grounds of theoretical considerations, is supported by the data presented here and it can be derived from the assumption of an exponentially declining hazard component added to a hazard component with a Gaussian shape. Under a simple competing risks model, less than 20 percent of feto-infant deaths during the one-year follow-up from the age of fetal viability are contributed by the "birth hump." Notably, among the conception cohort of non-Hispanic Black maternal origin, this contribution is only 9 percent, while the general level of feto-infant mortality is much higher among this

⁴ In quite a real sense if one considers the images generated from a 3D ultrasound.

stratum compared to the population average. This suggests that the "hump" is an additive phenomenon, which in turn implies an increasing share of deaths during or shortly after labor on all fetal and infant death as feto-infant mortality continues to decline.

Risks associated with the transition of birth: A formidable challenge for future research is to connect the aggregate phenomenon of the "birth-hump" to the transitional shock experienced by an individual as it moves from the intrauterine environment into infancy. In perinatal epidemiology, the same estimation problem is motivated by the desire to maximize the survival chances of an unborn child. Should labor be induced at a given age of gestation, or is it better to wait until labor sets in naturally? At heart lies the question of the risk of death prior to and after delivery, but such a change in risk can only ever be estimated indirectly as no one born alive ever died in utero. Current approaches to calculating the "risk of birth" thus are based on the strong assumption that children born in a given week of gestation t experienced the same risk of fetal death as the complete cohort of unborn children until t. But given that some fetal conditions are associated with a higher risk of stillbirth, pre-term birth, and infant death, this assumption must be deemed very crude, and instead, one would expect prematurely born infants to have had a higher risk of fetal death compared to infants born on full-term. Including exactly those information on fetal condition into the model, which are strongly associated with the timing of birth as well as fetal and infant death, would alleviate this issue and allow for a more precise estimate of the change in mortality across the feto-infant transition conditional on the timing of birth. The methodological framework for such an analysis could be given by the multi-timescale and multi-state approach to survival analysis, as proposed by Iacobelli and Carstensen (2013).

A. Description of methods

Determining gestational age

For the purposes of this paper, a key field on the birth and death certificates is the estimated age of gestation upon delivery as a proxy for the length of a pregnancy. This measure is subject to certain biases, which are crucial to keeping in mind when interpreting the results. Gestational age is defined as the weeks since the first day of the last menstrual period of the mother (LMP) and commonly measured by subtracting the date at LMP as reported by the women from the date of (still-)birth. This method suffers from recall bias, which may lead to digit preference in the reported dates. An alternative ist to derive the age of a pregnancy from ultrasound measurements of the unborn child. While the ultrasound method generally allows for a more precise estimate of the date of life-birth, it can be systematically biased in cases where the fetus is growth restricted. As abnormal fetal growth is a risk factor for fetal death, the gestational age at stillbirth may be severely biased under the ultrasound method. Additionally, the age of gestation at fetal death is positively biased by the time-lag between intrauterine death and the delivery of the dead fetus, which in-part explains the observation of fetal deaths at the implausible gestational ages of 46 and 47 weeks. In analyzing the age pattern of feto-infant mortality, we will utilize the gestational ages at delivery as they are reported on the birth and fetal death certificates and point out the role of the aforementioned biases whenever they are relevant for the interpretation of the results.

Delineating conception cohorts

When considering the survival of fetuses into infancy, a straightforward definition of a cohort is all subjects who have been conceived during the same time period, i.e., a "conception cohort." To determine the year of conception *y* for every single subject in the data we subtract the estimated weeks of gestation at delivery from the date at delivery and add two weeks to account for the average delay between the date of the last menstrual period of the mother (the time origin of the gestational age) and the date of fertilization. In this paper, we compare conception cohorts 1989, 1999, 2009.

Assembling the multi-state feto-infant life table

After delineating the conception cohorts y and determining N_{24}^F , the number of fetuses at risk at the start of observation, we calculate a multi-state feto-infant life table across the five states of fetus F, neonate N, post-neonate P, dead D and censored C. This requires the aggregation of transition counts T among states over age. For each single week of gestation let $T_t^{F \to D}$ denote the number of fetal deaths, $T_t^{F \to N}$ the number of births, $T_t^{N \to D}$ the number of neonatal deaths, $T_t^{N \to P}$ the number of recent survivors of the first week of life, $T_t^{P \to D}$ the number of post-neonatal deaths, and $T_t^{P \to C}$ the number of censorings

at week 77. The fetal, neonatal and post-neonatal population at risk at the beginning of gestational age t are then given by the recurrence equations

$$\begin{split} N_t^F &= N_{t-1}^F - T_{t-1}^{F \to D} - T_{t-1}^{F \to N}, \\ N_t^N &= N_{t-1}^N + T_{t-1}^{F \to N} - T_{t-1}^{N \to D} - T_{t-1}^{N \to P}, \\ N_t^P &= N_{t-1}^P + T_{t-1}^{N \to P} - T_{t-1}^{P \to D} - T_{t-1}^{P \to C}. \end{split}$$

To calculate the population exposures, we assume a uniform distribution of births and fetal deaths within each week of gestation where E_t^F is the total time spent in the fetal state over week of gestation t by the conception cohort under observation. The exposure times for the neonate and post-neonate state, E_t^N and E_t^P , are additionally informed by the chronological age of the infant at the time of transition measured in days.

Writing $S = \{F, N, P\}$ for the set of fetal, neonatal and post-neonatal states with $s \in S$ we calculate, for every week t, state-specific mortality rates $m_t^{s \to D} = \frac{T_t^{s \to D}}{E_t^s}$, total exposure times $E_t = \sum_S E_t^s$, state-specific relative exposures $p_t^s = \frac{E_t^s}{E_t}$, the combined feto-infant mortality rate $\overline{m}_t = \sum_s m_t^{s \to D}$. The empirical distribution of life-births given by $\pi_t^{F \to N} = \frac{T_t^{F \to N}}{\sum_t T_t^{F \to N}}$.

Expressing the combined feto-infant mortality rate at week of gestation t as a weighted average of fetal-, neonatal-, and post-neonatal mortality rates, $m_t = \sum_S p_t^s m_t^{s \to D}$ allows to explain the birth hump in terms of the shifting population proportions and mortality rates among the three groups over time. An application of the Kitagawa decomposition [Kitagawa1955] to the difference in feto-infant mortality between weeks t_1 and t_2 yields

$$\Delta \overline{m}_{t_1,t_2} = \underbrace{\sum_{S} \frac{p_{t_1}^s + p_{t_2}^s}{2} \Delta m_{t_1,t_2}^s}_{\Delta r = \Delta r^F + \Delta r^F} + \underbrace{\sum_{S} \frac{m_{t_1}^s + m_{t_2}^s}{2} \Delta p_{t_1,t_2}^s}_{\Delta c = \Delta c^F + \Delta c^N + \Delta c^P}$$

The approach of further decomposing the rate component Δr and the compositional component Δc in their sub-population contributions Δr^F , Δr^N , Δr^F , and Δc^F , Δc^N , Δc^F has been proposed by (Chevan and Sutherland 2009).

A latent competing risks model of feto-infant mortality

In order to describe the shape and magnitude of the apparent "birth hump," it is useful to separate the feto-infant hazard trajectory into two components: a monotonically declining "ontogenescent hazard" h^{O} and a hump-shaped "transitional hazard" h^{T} . Both sources of risk add up to

$$h(x) = h^{O}(x) + h^{T}(x),$$
 (1)

the total hazard of feto-infant death at gestational age t = x + 24, where x measures the weeks since fetal viability. The primary purpose of model (1) is to facilitate comparisons

between populations by providing a parsimonious and informative parametrization of the feto-infant mortality trajectory, and to that end, we choose simple parametric expressions for both components. A negative-Gompertz hazard,

$$h^{\mathcal{O}}(x) = a_1 \exp(-bx),$$

captures the overall trend of log-linearly declining feto-infant mortality over weeks of gestation with a_1 being the level of the ontogenescent hazard at fetal viability, and *b* the rate of ontogenescence, that is the relative rate of feto-infant mortality decline over the 52 weeks post-viability when any excess mortality contributed by the birth hump has been separated out.

The transitional hazard component reflecting the "birth hump" is specified to follow the kernel of a normal distribution resulting in the "Gaussian" hazard

$$h^{\mathrm{T}}(t) = a_2 \exp\left(-\frac{(t-c)^2}{2\sigma^2}\right),$$

scaled by a_2 , which measures the mortality level at the mode of the hump at age x = c. The width of the hump is controlled via parameter σ with larger values resulting in flatter peaks.

The above decomposition of the overall hazard of feto-infant death into two components follows a long tradition of "competing risks" modeling of population mortality (Makeham1867, Siler1979, Heligman1980, Remund2018) where the overall risk of death is the sum of cause-specific hazards, each following a different age-trajectory. This begs the question about the nature of the risks competing with each other. The defining feature of the ontogenescent component is the continuous decline in hazard. Potential prenatal drivers of this decline are conditions that tend to lead to early fetal death such as severe congenital anomalies, e.g., anencephaly, or complications of fetal health that are all the more lethal, the earlier in pregnancy they occur, such as in-utero infection, placental dysfunction or abruption, abnormalities of the umbilical cord or rupture of the uterus. Correlated with these conditions is the risk of pre-term delivery, either induced in an attempt to save the fetus, or spontaneous. In either case, the survival chances of the pre-term child improve dramatically with the age of gestation. The post-term decline in the hazard of death may result from the continuing maturity of the cohort of infants and their increasing ability to resist the challenges posed by infection and accidents as well as the successful management of congenital malformations and chronic health conditions. Hazards due to complications of labor in late pre-term or term infants are captured by the transitional component and may be strictly birth-related such as intrapartum asphyxia or birth trauma or the consequence of severe fetal malformations that do not allow for survival outside of the uterus.

The feto-infant mortality trajectory informs about the development of a cohort's mortality risk, as its member's transition into life. Complementary to this risk perspective is the incidence of feto-infant death as measured by the probability of fetal- or infant death within x weeks following fetal-viability. The cumulative incidence of feto-infant death can be derived from the two hazard components via the well-known relationship

$$F(x) = 1 - \exp\left(-\int_0^x h(s) \, \mathrm{d}s\right) = 1 - \exp\left(-\int_0^x h^O(s) + h^T(s) \, \mathrm{d}s\right).$$

Level, ontogenescent and transition components of mortality differentials

Evaluating F(x) at x = 52 gives the probability of fetal or infant death within one year of reaching the age of fetal viability, and thus F(52) is a summary measure of adverse pregnancy outcomes combining fetal and infant deaths. The difference in F(52) between two populations may be decomposed into three effects: 1) differences due to different levels of feto-infant mortality as measured by parameter a_1 , 2) ontogenescent differences due to different rates of mortality decline over age of gestation as measured by parameter b, and 3) transitional differences due to the different magnitude, location and shape of the birth hump as measured by parameters a_2 , c and σ . Given parameter vector $\theta = (a_1, b, a_2, c, \sigma)$, for populations A and B, we perform a Horiuchi decomposition (Horiuchi et al. 2008) to explain how the between-population difference in each parameter contributes to the overall difference $F(52, \theta_A) - F(52, \theta_B)$. The level and ontogenescent contributions to the difference in one-year survival are given by the a_1 and b parameter contributions respectively whereas the a_2 , c, and σ contributions sum up to the transitional contribution, e.g., the difference in one-year survival due to difference in the magnitude, location, and shape of the birth hump.

Competing risks inference

How many members of a cohort fail to overcome the "birth hump" on their way to infancy? Following the calculus of competing-risks, one can derive the share of infant deaths contributed by the transitional hazard. The cumulative probability of feto-infant death due to causes associated with the transitional component is $F^T(x) = \int_0^x S(s)h^T(s) ds$ which can be evaluated using numerical integration techniques. The share of deaths attributable to the transitional hazard up until post-viability age *x* then is $\rho(x) = F^T(x)/F(x)$.

Censored likelihood

We fit model (1) via maximum likelihood with the likelihood function constructed from the probability of observing D_j fetal or infant deaths in age group j given model parameters $\theta = (a_1, b, a_2, c, \sigma)$, written as $D_j[S(x_j|\theta) - S(x_{j+1}|\theta)]$, and the probability of observing C_j censored survivors at the end of age group j, $C_jS(x_j + 1|\theta)$, hence reflecting the fact

that observations are both interval-censored, as the timing of combined fetal and infant deaths is only known to lie within some week of gestation, and right-censored, because observation stops one year after fetal-viability when most members of a cohort are still alive. Taking the product over all age groups j = 1 : J yields the likelihood function

$$L(\boldsymbol{\theta}|D_j, C_j) = \prod_j \left[S(x_j|\boldsymbol{\theta}) - S(x_{j+1}|\boldsymbol{\theta}) \right]^{D_j} S(x_{j+1}|\boldsymbol{\theta})^{C_j},$$

with corresponding log-likelihood

$$\log L(\boldsymbol{\theta}|D_j, C_j) = \sum_j D_j \log \left[S(x_j|\boldsymbol{\theta}) - S(x_{j+1}|\boldsymbol{\theta}) \right] + C_j \log S(x_{j+1}|\boldsymbol{\theta}).$$

B. The nosplit algorithm for memory-efficient aggregation of event history data

The state-of-the-art for aggregation of multi-state life history data into age-period and cohort intervals is the "split-aggregate" method, whereby first, the individual level dataset is expanded into a single row per individual per time interval visited. In a second step, transition counts and state occupancy times per time interval are calculated from this expanded data set. The split step expands an already large data set even further and thus can be extremely costly in memory usage and processor time.

We present an episode-split free method to aggregate multi-state life-history data into time intervals. The "nosplit-aggregate" method first produces three summary tables from the unaltered individual-level data set and then derives the interval and state-specific risk sets, exposure times, and transition counts via elementary calculations on the aggregated tables.

The code listing below gives an implementation of nosplit in the R language (R Core Team 2020).

```
# Aggregate Transitions Counts and Occupancy Times
1
2
    # Episode-split-free Risk-set and Exposure Time Calculation
3
4
    # from Event History Data
5
    # @param df
6
    # A data frame.
7
   # @param t_in
8
   # Entry time into state.
9
   # @param d_in
10
    # State being entered.
11
   # @param t_out
12
   # Exit time from state.
13
   # @param d_out
14
   # State being exited into.
15
   # @param breaks
16
    # A numeric vector of break points for time-scale.
17
   # @param wide
18
    # Output table in wide format (default=TRUE)?
19
    # @param closed_left
20
        Time intervals closed to the left and open to the right (default=TRUE)?
21
    #
    # @param disable_input_checks
22
    #
        Should input checks be disabled (default=FALSE)?
23
    #
24
    # @return
25
    # A data frame with columns
26
    #
          orig: origin state
27
    #
          i: age group index
28
    #
         x: starting age of j
29
        n: width of j
    #
30
        Z: number of entries into origin state during jW: number of exits from origin state during j
    #
31
32
    #
        P:
0:
                population number in origin state at beginning of j
    #
33
    #
                total observation time of population visiting origin state in j
34
         (if wide = FALSE)
    #
35
```

```
dest: destination state
    #
36
    #
           W_k: number of exits from origin state to destination state during j
37
    #
           (if wide = TRUE)
38
           to_*: number of exits from origin state to state * during j
39
    #
    AggregateStateTransitions <- function (</pre>
40
      df.
41
      t_in, d_in, t_out, d_out,
42
      breaks,
43
      wide = TRUE, drop0exp = TRUE,
44
      closed_left = TRUE,
45
46
      disable_input_checks = FALSE
    ) {
47
48
      require(tidyverse)
49
50
      t_in = enquo(t_in); d_in = enquo(d_in);
51
      t_out= enquo(t_out); d_out = enquo(d_out)
52
53
      # input checks
54
55
      if (identical(disable_input_checks, FALSE)) {
56
         # check if all transition times are contained in
57
         # range of breaks
58
         t_range = c(min(pull(df, !!t_in)), max(pull(df, !!t_out)))
59
         breaks_range = range(breaks)
60
         if ( identical(closed_left, TRUE) ) {
61
           if (any(
62
             t_range[1] < breaks_range[1] |</pre>
63
             t_range[2] >= breaks_range[2]
64
           )) {
65
             stop(paste0(
66
                'Transition time outside range of breaks. Ensure that all t_ >='),
67
               breaks_range[1], ' and <', breaks_range[2]</pre>
68
69
             )
           }
70
         }
71
         if ( identical(closed_left, FALSE) ) {
72
           if (any(
73
             t_range[1] <= breaks_range[1] |</pre>
74
             t_range[2] > breaks_range[2]
75
           )) {
76
             stop(paste0(
77
                'Transition time outside range of breaks. Ensure that all t_ >'),
78
               breaks_range[1], ' and <=', breaks_range[2]</pre>
79
80
             )
           }
81
        }
82
      }
83
84
      # total number of age intervals
85
86
      J_ = length(breaks)-1
      # index of age intervals
87
      j_{-} = 1:J_{-}
88
      # width of age intervals
89
      n_j = diff(breaks)
90
      # unique origin states
91
```

```
k_in_ = unique(pull(df, !!d_in))
92
       # unique destination states
03
       k_out_ = unique(pull(df, !!d_out))
94
05
       # find the index of an interval defined by
96
       # <breaks> each element in <x> is contained in
97
       # returns NA if x outside breaks
98
       FindIntervalJ <-</pre>
99
         function (x, breaks, cl = closed_left) {
100
           if (identical(cl, TRUE)) {
101
102
             # [a, b)
             right = FALSE; lowest = FALSE
103
           } else {
104
             # (a, b] with [a0, b0]
105
             right = TRUE; lowest = TRUE
106
           }
107
           .bincode(
108
             x = x, breaks = breaks,
109
             right = right, include.lowest = lowest
110
           )
111
         }
112
113
       # 1. Aggregation
114
115
       # tabulate exits by age, origin and destination state
116
       W_k_tab <-
117
         df %>%
118
         select(t_out = !!t_out, d_in = !!d_in, d_out = !!d_out) %>%
119
         mutate(
120
           # add age interval index to each exit
121
           j = FindIntervalJ(pull(., t_out), breaks, closed_left),
122
123
         ) %>%
         # for each observed combination of
124
125
         # age and
         # origin state and
126
         # destination state...
127
         group_by(d_in, d_out, j) %>%
128
         summarise(
129
           # ...total number of exits
130
           W_k = n(),
131
           # total time lost in age due to exit
132
           Lw_k = sum(breaks[j+1]-t_out)
133
         ) %>%
134
         ungroup()
135
136
       # tabulate exits by age and origin state
137
       # based on prior tabulation on destination specific exits
138
       W tab <-
139
         W_k_tab %>%
140
         # for each observed combination of
141
142
         # age and
143
         # origin state...
         group_by(j, d_in) %>%
144
         summarise(
145
           # ...total exits
146
           W = sum(W_k),
147
```

```
# ...total time lost in interval due to exit
148
           Lw = sum(Lw_k)
140
         ) %>%
150
         ungroup() %>%
151
         # add rows for missing combinations
152
         # of age interval and origin state
153
         complete(
154
           d_{in} = k_{in}, j = j_{,}
155
           fill = list(W = 0, Lw = 0)
156
157
         )
158
       # tabulate entries by age and state entered into
159
       Z tab <-
160
         df %>%
161
         select(d_in = !!d_in, t_in = !!t_in) %>%
162
163
         mutate(
            j = FindIntervalJ(pull(., t_in), breaks, closed_left),
164
         ) %>%
165
         group_by(j, d_in) %>%
166
         summarise(
167
           # ...total entries
168
           Z = n(),
169
           # ...total entries right at start of interval
170
           Z0 = sum(t_in==breaks[j]),
171
           # ...total time lost in interval due to late-entry
172
           Lz = sum(t_in-breaks[j])
173
         ) %>%
174
175
         ungroup() %>%
         complete(
176
           d_{in} = k_{in}, j = j_{,i}
177
           fill = list(Z = 0, Z0 = 0, Lz = 0)
178
179
         )
180
181
       # tabulate concurrent entries and exits by interval
       ZW_tab <-
182
         df %>%
183
         select(t_in = !!t_in, t_out = !!t_out, d_in = !!d_in) %>%
184
185
         # aggregate individual level entry
         # and exit times into predefined age groups
186
         mutate(
187
           # add interval index to each entry
188
           j = FindIntervalJ(pull(., t_in), breaks, closed_left),
189
           # are entries and exits in same interval?
190
           zw = j == FindIntervalJ(pull(., t_out), breaks)
191
192
         ) %>%
         # for each combination of
193
         # state and
194
         # interval
195
196
         group_by(d_in, j) %>%
         summarise(
197
198
           # ...total concurrent entries and exits
           # there may be NAs in logic vector <zw> when
199
           # and entry or exit falls outside the range
200
           # of all intervals. as those cases don't have to
201
            # be counted na.rm=TRUE is applied
202
           ZW = sum(zw, na.rm = TRUE)
203
```

```
) %>%
204
         ungroup() %>%
205
         complete(
206
           d_{in} = k_{in}, j = j_{,i}
207
           fill = list(ZW = 0)
208
         )
209
210
       # 2. Determine risk-sets and exposure times
211
212
       # exit counts for all possible combinations
213
       # of origin state, destination state and
214
       # age interval
215
       # intrastate transitions are 0 now
216
       # but are added later
217
       W_k_tab_complete <-
218
         W_k_tab %>%
219
         select(-Lw_k) %>%
220
         complete(
221
           d_in = k_in_, d_out = k_out_, j = j_,
222
           fill = list(W_k = 0)
223
         )
224
225
       # occurence-exposure table
226
       oe_tab <-
227
         bind_cols(W_tab, Z_tab[,-(1:2)], ZW_tab[,-(1:2)]) %>%
228
229
         mutate(
           x = breaks[j],
230
231
           n = n_j[j]
         ) %>%
232
         # for each entry state...
233
         group_by(d_in) %>%
234
235
         mutate(
           # number of observations entering j via j-1
236
237
           \# R_{(j+1)} = R_{j} + Z_{j} - W_{j}
           R = c(0, head(cumsum(Z) - cumsum(W), -1)),
238
           # population at risk at x_j
239
           P = R + Z0,
240
           # number of observations in j that did neither start
241
           # nor end during j
242
           Q = R - W + ZW,
243
           # number of observations entering i
244
           # that do not end during j
245
           U = Z - ZW,
246
           # total observation time during j
247
           0 = Q^{*}n + (Z + W - ZW)^{*}n - Lz - Lw,
248
           # number of intrastate transitions
249
           I = Q + U,
250
         ) %>%
251
252
         ungroup() %>%
         left_join(W_k_tab_complete, by = c('d_in', 'j')) %>%
253
254
         # intrastate transitions
         mutate(
255
           W_k = ifelse(d_in == d_out, I, W_k)
256
         ) %>%
257
         select(orig = d_in, dest = d_out, j, x, n, Z, W, P, 0, W_k)
258
259
```

```
# drop intervals with 0 exposure
260
       if (identical(drop0exp, TRUE)) {
261
         oe_tab <-
262
           oe_tab %>%
263
           filter(0 > 0)
264
       }
265
266
       # convert to wide format
267
       if (identical(wide, TRUE)) {
268
         oe_tab <-
269
           oe_tab %>%
270
           mutate(dest = paste0('to_', dest)) %>%
271
           spread(key = dest, value = W_k)
272
       }
273
274
       return(oe_tab)
275
276
    }
277
```

C. Tables of parameter estimates

 Table 4:
 Table of estimated parameters of feto-infant hazard trajectory over gestational age by sex.

a_1 b a_2 c σ	Male 4.9e-4 (4.8e-4, 5.1e-4) 6.7e-2 (6.5e-2, 6.8e-2) 2.5e-4 (2.3e-4, 2.6e-4) 1.4e+1 (1.4e+1, 1.4e+1) 2.4e+0 (2.2e+0, 2.6e+0)	Female 4.5e-4 (4.3e-4, 4.6e-4) 7.1e-2 (7.0e-2, 7.3e-2) 2.4e-4 (2.2e-4, 2.6e-4) 1.4e+1 (1.4e+1, 1.5e+1) 2.3e+0 (2.2e+0, 2.5e+0)
$F(52) \times 10e5$	864 (851, 878)	751 (739, 763)
$F(52)^{-1}$	116 (114, 118)	133 (131, 135)
$\rho(52)\%$	17.0 (15.9, 18.2)	18.4 (16.9, 19.7)

	1989	1999	2009
a_1	6.4e-4 (6.3e-4, 6.5e-4)	5.7e-4 (5.6e-4, 5.8e-4)	4.7e-4 (4.6e-4, 4.8e-4)
b	6.2e-2 (6.1e-2, 6.2e-2)	7.1e-2 (7.0e-2, 7.2e-2)	6.9e-2 (6.8e-2, 7.0e-2)
a_2	3.5e-4 (3.4e-4, 3.6e-4)	3.4e-4 (3.2e-4, 3.5e-4)	2.4e-4 (2.3e-4, 2.5e-4)
c	1.5e+1 (1.5e+1, 1.6e+1)	1.5e+1(1.4e+1, 1.5e+1)	1.4e+1 (1.4e+1, 1.4e+1)
σ	2.5e+0 (2.4e+0, 2.6e+0)	2.3e+0 (2.3e+0, 2.4e+0)	2.4e+0 (2.2e+0, 2.5e+0)
$F(52) \times 10e5$	1,207 (1,196, 1,219)	979 (969, 990)	809 (800, 818)
$F(52)^{-1}$	82.8 (82.1, 83.6)	102 (101, 103)	124 (122, 125)
o(52)%	18.0 (17.3, 18.7)	20.1 (19.2, 21.0)	17.6 (16.7, 18.5)

 Table 5:
 Table of estimated parameters of feto-infant hazard trajectory over gestational age by conception cohort.

 Table 6:
 Table of estimated parameters of feto-infant hazard trajectory over gestational age by maternal origin.

a_1 b a_2 c σ	non-Hispanic Black	Hispanic	Non-Hispanic White
	9.0e-4 (8.7e-4, 9.4e-4)	4.0e-4 (3.8e-4, 4.2e-4)	3.7e-4 (3.6e-4, 3.8e-4)
	7.0e-2 (6.8e-2, 7.3e-2)	7.1e-2 (6.8e-2, 7.4e-2)	6.5e-2 (6.3e-2, 6.6e-2)
	2.4e-4 (2.1e-4, 2.8e-4)	2.3e-4 (2.0e-4, 2.6e-4)	2.3e-4 (2.2e-4, 2.5e-4)
	1.4e+1 (1.4e+1, 1.4e+1)	1.4e+1 (1.4e+1, 1.4e+1)	1.4e+1 (1.4e+1, 1.5e+1)
	2.1e+0 (1.7e+0, 2.5e+0)	2.6e+0 (2.4e+0, 2.9e+0)	2.4e+0 (2.3e+0, 2.6e+0)
$F(52) \times 10e5$	1,364 (1,332, 1,399)	698 (679, 719)	695 (684, 705)
$F(52)^{-1}$	73.3 (71.5, 75.1)	143 (139, 147)	144 (142, 146)
$\rho(52)\%$	9.2 (7.5, 11.0)	21.5 (18.7, 24.4)	20.4 (19.1, 21.7)

Table 7: Shape decomposition of differences in F(52) between the sexes.

	Male - Female
$\Delta F(52) \times 10e5$	113 [95.3, 131]
Level contribution	62.1 [33.9, 89.2]
Ontogenescent contribution	41.4 [20.9, 61.2]
Birth hump contribution	9.23 [-5.67, 23.7]
$\Delta F(52)$ %	15.0 [12.6, 17.8]

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Table 8: Shape decomposition of differences in F(52) between the conception cohorts.

	1989 - 1999	1999 - 2009
$\Delta F(52) \times 10e5$	-228 [-244, -213]	-170 [-183, -156]
Level contribution	-97 [-121, -74.2]	-136 [-156, -116]
Ontogenescent contribution	-109 [-126, -92]	20.1 [6.0, 34.2]
Birth hump contribution	-21 [-33.8, -9.2]	-54.0 [-65.1, -42.8]
$\Delta F(52)$ %	-18.9 [-20.1, -17.8]	-17.4 [-18.6, -16.1]

Table 9: Shape decomposition of differences in F(52) between maternal ethnicities.

	non-Hispanic Black - White	Hispanic - White	Hispanic - non-Hispanic Black
$\Delta F(52) \times 10e5$	668 (637, 701)	3.3 (-18.6, 25.4)	-665 (-701, -630)
Level contribution	747 (704, 797)	41.7 (10.3, 75.8)	-680 (-738, -623)
Ontogenescent contribution	-63.5 (-92.9, -35.0)	-46.9 (-72.3, -20.5)	-8.8 (-50.6, 32.7)
Birth hump contribution $\Delta F(52)\%$	-15.2 (-40.5, 11.9)	8.5 (-12.7, 32.8)	23.7 (-8.2, 56.7)
	96.4 (91.2, 102)	0.04 (-2.7, 3.7)	-48.8 (-50.7, -47.0)

ICD10	Category
A, B, P008, P351-P399, Y430-Y848	Infections, parasites and surgery
C, D151-D489, Q174-Q189, Q359-Q564, Q611-Q623, Q641-Q809, Q832-Q859, Q891-Q894	Congenital malformations and neoplasms (less severe)
Q00-Q079, Q200-Q349, Q600-Q606, Q631-Q639, Q811-Q829, Q860-Q878, Q897-Q999	Congenital malformations and neoplasms (severe)
P00-P007, P009-P019	Maternal complications
P020-P049, P103-P159, P230-P249	Placenta, cord, membrane and labour complications
P050-P082, P250-P289	Prematurely
P950	Unspecific stillbirth
R950-R990	Sudden infant death
D550-D899, E, F, G, H, I, J, K, L, M, N, P200-P209, P501-P942, P60-P960, R02-R788	Other
V, X, Y000-Y340	Accidents & Violence

Table 10: Cause of death categorization.

References

- L. S. Bakketeig, D. G. Seigel, and P. M. Sternthal. A fetal-infant life table based on single births in Norway, 1967–1973. *American Journal of Epidemiology*, 107(3):216–225, 1978. doi:10.1093/oxfordjournals.aje.a112528.
- E. Barbi, F. Lagona, M. Marsili, J. W. Vaupel, and K. W. Wachter. The plateau of human mortality: Demography of longevity pioneers. *Science*, 360(6396):1459–1461, 2018. doi:10.1126/science.aat3119.
- S. Berrut, V. Pouillard, P. Richmond, and B. M. Roehner. Deciphering infant mortality. *Physica A: Statistical Mechanics and its Applications*, 463:400–426, 2016. doi:10.1016/j.physa.2016.07.031.
- J. Bourgeois-Pichat. La mesure de la mortalité infantile. II. les causes de décès. *Population*, 6(3):459–480, 1951. doi:10.2307/1523958.
- E. Carlson, J. M. Hoem, and J. Rychtarikova. Trajectories of fetal loss in the czech republic. *Demography*, 36(3):327–37, 1999. doi:10.2307/2648056.
- A. Chevan and M. Sutherland. Revisiting Das Gupta: Refinement and extension of standardization and decomposition. *Demography*, 46(3):429–449, 2009. doi:10.1353/dem.0.0060.
- CIOMS Working Groups III and V. Guidelines for preparing core clinical-safety information on drugs. Technical report, Geneva, 1999.
- M. Ebeling. How has the lower boundary of human mortality evolved, and has it already stopped decreasing? *Demography*, 55(5):1887–1903, 2018. doi:10.1007/s13524-018-0698-z.
- G. B. Feldman. Prospective risk of stillbirth. *Obstetrics and Gynecology*, 79(4):547–553, 1992.
- F. E. French and J. M. Bierman. Probabilities of fetal mortality. *Public Health Reports*, 77(10):835–47, 1962. doi:10.2307/4591645.
- C. Galley and R. Woods. On the distribution of deaths during the first year of life. *Population*, 11(1):35–60, 1999.
- J. Gampe. Human mortality beyond age 110. In H. Maier, J. Gampe, B. Jeune, J.-M. Robine, and J. W. Vaupel, editors, *Supercentenarians*, Demographic Research Monographs, pages 219–230. Springer, Berlin, 2010. ISBN 978-3-642-11519-6. doi:10.1007/978-3-642-11520-2_13.
- M. K. Goldhaber and B. H. Fireman. The fetal life table revisited: Spontaneous abortion rates in three kaiser permanente cohorts. *Epidemiology*, 2(1):33–39, 1991. doi:10.1097/00001648-199101000-00006.
- J. R. Goldstein. A secular trend toward earlier male sexual maturity: evidence from shifting ages of male young adult mortality. *PloS one*, 6(8):e14826, 2011. doi:10.1371/journal.pone.0014826.

- B. Gompertz. On the nature of the function expressive of the law of human mortality, and on a new mode of determining the value of life contingencies. *Philosophical Transactions of the Royal Society of London*, 115:513–583, Dec. 1825. doi:10.1098/rstl.1825.0026.
- A. E. Greb, R. M. Pauli, and R. S. Kirby. Accuracy of fetal death reports: comparison with data from an independent stillbirth assessment program. *American Journal of Public Health*, 77(9):1202–1206, 1987. doi:10.2105/ajph.77.9.1202.
- S. Horiuchi and J. R. Wilmoth. Deceleration in the age pattern of mortality at older ages. *Demography*, 35:391, 1998. ISSN 0070-3370. doi:10.2307/3004009.
- S. Horiuchi, J. R. Wilmoth, and S. D. Pletcher. A decomposition method based on a model of continuous change. *Demography*, 45(4):785–801, 2008. doi:10.1353/dem.0.0033.
- S. Iacobelli and B. Carstensen. Multiple time scales in multi-state models. *Statistics in Medicine*, 32(30):5315–5327, 2013. doi:10.1002/sim.5976.
- N. Isaacson. The "fetus-infant": Changing classifications of in utero development in medical texts. *Sociological Forum*, 11(3):457–480, 1996. doi:10.1007/bf02408388.
- K. Joseph. Incidence-based measures of birth, growth restriction, and death can free perinatal epidemiology from erroneous concepts of risk. *Journal of Clinical Epidemiology*, 57(9):889–897, 2004. doi:10.1016/j.jclinepi.2003.11.018.
- K. S. Joseph. Theory of obstetrics: An epidemiologic framework for justifying medically indicated early delivery. *BMC Pregnancy and Childbirth*, 7(1), 2007. doi:10.1186/1471-2393-7-4.
- E. M. Kitagawa. Components of a difference between two rates. *Journal of the American Statistical Association*, 50(272):1168–1194, 1955. doi:10.1080/01621459.1955.10501299.
- F. B. Kristensen and F. Mac. Life table analysis of infant mortality and feto-infant mortality distributed on causes of death in Denmark 1983-1987. *International Journal* of Epidemiology, 21(2):320–3, 1992. doi:10.1093/ije/21.2.320.
- D. A. Levitis. Before senescence: the evolutionary demography of ontogenesis. Proceedings of the Royal Society B, 278(1707):801–809, 2011. doi:10.1098/rspb.2010.2190.
- J. A. Martin and D. L. Hoyert. The national fetal death file. *Seminars in Perinatology*, 26 (1):3–11, 2002. doi:10.1053/sper:2002.29834.
- National Center for Health Statistics. Birth cohort linked birth-infant death data files (U.S. data), 2016a. URL ftp://ftp.cdc.gov/pub/Health_Statistics/NCHS/Datasets/DVS/ cohortlinkedus/.
- National Center for Health Statistics. Fetal death data files (U.S. data), 2016b. URL ftp://ftp.cdc.gov/pub/Health_Statistics/NCHS/Datasets/DVS/fetaldeathus/.
- W. Perks. On some experiments in the graduation of mortality statistics. *Journal of the Institute of Actuaries*, 63(1):12–57, 1932.

- R. W. Platt, K. S. Joseph, C. V. Ananth, J. Grondines, M. Abrahamowicz, and M. S. Kramer. A proportional hazards model with time-dependent covariates and time-varying effects for analysis of fetal and infant death. *American Journal of Epidemiology*, 160(3):199–206, 2004. doi:10.1093/aje/kwh201.
- R Core Team. *R: A Language and Environment for Statistical Computing*. R Foundation for Statistical Computing, Vienna, Austria, 2020. URL https://www.R-project.org/.
- A. Remund, C. G. Camarda, and T. Riffe. A cause-of-death decomposition of young adult excess mortality. *Demography*, 55(3):957–978, 2018. doi:10.1007/s13524-018-0680-9.
- I. Seri and J. Evans. Limits of viability: definition of the gray zone. *Journal of Perinatology*, 28:S4–S8, Apr. 2008. doi:10.1038/jp.2008.42.
- S. Shapiro, E. W. Jones, and P. M. Densen. A life table of pregnancy terminations and correlates of fetal loss. *The Milbank Memorial Fund Quarterly*, 40(1):7, 1962. doi:10.2307/3348609.
- G. C. S. Smith. Life-table analysis of the risk of perinatal death at term and post term in singleton pregnancies. *American Journal of Obstetrics and Gynecology*, 184(3): 489–496, 2001. doi:10.1067/mob.2001.109735.
- G. C. S. Smith. Estimating risks of perinatal death. *American Journal of Obstetrics and Gynecology*, 192(1):17–22, 2005. doi:10.1016/j.ajog.2004.08.014.
- T. N. Thiele. On a mathematical formula to express the rate of mortality throughout the whole of life, tested by a series of observations made use of by the Danish Life Insurance Company of 1871. *Journal of the Institute of Actuaries*, 16(5):313–329, 1871. doi:10.1017/s2046167400043688.
- J. W. Vaupel. Trajectories of mortality at advanced ages. In K. W. Wachter and C. E. Finch, editors, *Between Zeus and the Salmon: The Biodemography of Longevity*, chapter 2, pages 17–37. National Academy Press, Washington D.C., 1997. ISBN 0-309-05787-6.
- P. Williamson and R. I. Woods. A note on the fetal-infant mortality problem. *Journal of Biosocial Science*, 35(2):201–212, 2003. doi:10.1017/S0021932003002013.
- R. Woods. *Death before Birth*. Oxford University Press, 2009. ISBN 978–0–19–954275–8. doi:10.1093/acprof:oso/9780199542758.001.0001.
- World Health Organization. *Neonatal and Perinatal Mortality: Country, Regional and Global Estimates.* World Health Organization, 2006. ISBN 9241563206.
- P. L. Yudkin, L. Wood, and C. W. G. Redman. Risk of unexplained stillbirth at different gestational ages. *The Lancet*, 329(8543):1192–1194, 1987. doi:10.1016/S0140-6736(87)92154-4.